

Some more series tests, --

Key Learning: it is easier to show
convergence/divergence of a series
than to know the limit of a
convergent series.

$$10.6 / 1-16$$


Comparison Test

$a_k, b_k > 0$ assume $a_k > b_k$ for every k

I have to
know
1 of the
series

if $\sum a_k$ Converges so does $\sum b_k$

If $\sum b_k$ diverges
then $\sum a_k$ diverges

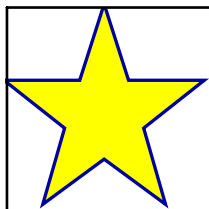
Limit Comparison test

Again, two positive-valued series, ...
I know about one-----

$$\text{Let } \lim_{k \rightarrow \infty} \frac{a_k}{b_k} = L$$

$$\text{if } L > 0$$

then both series converge
OR both series diverge



Ratio Test

 $a_1, a_2, \dots, a_k, a_{k+1}, \dots$

$$\text{Let } \lim_{k \rightarrow \infty} \left(\frac{a_{k+1}}{a_k} \right) = L$$

then: $L < 1 \Rightarrow$ series converges
 $L > 1 \Rightarrow$ series diverges
 $L = 1 \Rightarrow$ \forall DKN